



Ειδική Υπηρεσία Διαχείρισης και Εφαρμογής Δράσεων  
στους τομείς Έρευνας, Τεχνολογικής Ανάπτυξης και Καινοτομίας

ΕΝΙΑΙΑ ΔΡΑΣΗ ΚΡΑΤΙΚΩΝ ΕΝΙΣΧΥΣΕΩΝ  
ΕΡΕΥΝΑΣ, ΤΕΧΝΟΛΟΓΙΚΗΣ ΑΝΑΠΤΥΞΗΣ  
& ΚΑΙΝΟΤΟΜΙΑΣ

## ΕΡΕΥΝΩ – ΔΗΜΙΟΥΡΓΩ – ΚΑΙΝΟΤΟΜΩ

### ΕΝΟΤΗΤΑ ΕΡΓΑΣΙΑΣ 3: ΒΕΛΤΙΣΤΟΠΟΙΗΣΗ ΣΧΗΜΑΤΟΣ ΚΑΙ ΤΟΠΟΛΟΓΙΑΣ ΚΑΤΑΣΚΕΥΩΝ

#### Π3.2 Παρουσίαση σε συνέδριο

Κωδικός Έργου: **T1ΕΔΚ-05603**

Τίτλος Έργου: Ολιστική Υπολογιστική Πλατφόρμα  
Βελτιστοποίησης Υψηλών Επιδόσεων – HP-  
OCP

Φορείς: ΕΜΠ-ISAAR

Χρόνος: Από το πρόγραμμα: M24

Παράδοσης: Υλοποιήθηκε: M15 (Νοέμβριος 2019)





## High Performance Topology Optimization Computing Platform

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### ABSTRACT

One of the most challenging tasks in the construction industry nowadays, is to reduce the material demands and distribute, in the same time, the material among the structural system in the best possible way. Topology optimization is a design procedure that is increasingly used, to generate optimized forms of structures in several engineering fields. The current paper presents the Topology Optimization (TO) module of the High-Performance Optimization Computing Platform (HP-OCP) which focuses on civil engineering problems.

More specifically the SIMP method [1] is implemented and the topology optimization problem is solved by using both OC and MMA algorithms. The HP-OCP is a platform which evaluates several objective functions, such as the volume of the structure, the compliance etc. and can solve constrained or unconstrained structural optimization problems. The above libraries are developed in C#. The core of the platform is created in such way that it can be integrated with any CAE program that has OAPI. In the proposed work we used the structural analysis and design software SAP2000.

Lagaros et al. [2] presented a C# code that solves topology optimization problems, which are discretized with 3D solid elements, using SAP2000. One of the highlights of the proposed work is that the above module can be used for all kind of finite elements. Benchmark tests are presented with structures that are simulated by 2D plane-stress elements, 3D-solid elements and shell elements. Furthermore, it is independent of the type of the mesh, structured or unstructured, so both examples are presented. In addition, a tool in C# was developed in order to connect Rhino's plugin Grasshoppers with SAP2000. In that way more complicated geometries can be generated in the CAD program Rhino then the structural engineering problem can be formulated in SAP2000 and finally the above module can solve the topology optimization problem.

In the proposed work a powerful tool for both architects and civil engineers is introduced. The capabilities of the TO module of the HP-OCP are presented and several test cases are shown. The analysis and design of the structures are performed in SAP2000 software, in order to achieve a realistic result that could be a solution for a real-world structure.

### Acknowledgement

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### References

- [1] M.P. Bendsoe, O. Sigmund, *Material interpolations in topology optimization*, *Arch. Appl. Mech.* 69 1999.
- [2] N.D. Lagaros, N. Vasileiou, G. Kazakis, *A C# code for solving 3D topology optimization problems using SAP2000*. *Optimization and Engineering*, Springer, 2018.



# High Performance Topology Optimization Computing Platform

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# Topology Optimization

Commercial software applications

- Most of commercial software are integrated into mechanical engineering oriented analysis and design software.
- Optistruct (Altair), Tosca (ABAQUS and MSC Nastran), ANSYS, SOLIDWORKS
- TO of HP-OCP is independent of the static analysis software
- Developed in C# language in .NET framework
- Integration via OAPI, XML data exchange format, etc. with commercial CAE
- SAP2000 is presented

# Topology Optimization Formulation

## Mathematical Formulation

- Initial mesh, loads, boundary condition
- Objective function: compliance
- Design variable: density of elements( $x$ )
- Constraints: FEA, volume, limits of density
- Methods: SIMP, Level set, BESO
- Optimization Algorithm: OC, SLP, MMA



$$\min_x C(x) = F * U(x)$$

s.t.

$$F = K(x) * U$$

$$\sum_{e=1}^N x_e = V$$

$$0 \leq x_e \leq 1$$

# Topology Optimization Formulation

SIMP, OC, FILTER

- SIMP Formulation:  $E(x) = x^p E_0$
- Partial Derivative of Compliance with respect to the design variable:

$$\frac{\partial C(x)}{\partial x_e} = -u_e(x)^T \frac{\partial k_e(x)}{\partial x_e} u_e(x)$$

- Modified expression:

$$k_e(x_e) = x_e^p * k_e^0 \Leftrightarrow k_e^0 = \frac{k_e(x_e)}{x_e^p}, \quad \frac{\partial k_e(x_e)}{\partial x_e} = p * x_e^{p-1} * k_e^0 = p * x_e^{p-1} * \frac{k_e(x_e)}{x_e^p} = p * \frac{k_e(x_e)}{x_e},$$

$$\frac{\partial C(x)}{\partial x_e} = -u_e(x)^T * p * \frac{k_e(x)}{x_e} u_e(x) = -p \frac{F^T u_e(x)}{x_e} = -\frac{p * C_e}{x_e}$$

- In order to avoid checkerboard problem a filter is applied:  $H_{ij} = R - dist(i, j)$

# HP-TOCP Module

## General Structure

- Preprocessing, Iterative procedure.
- Delegates functions to retrieve necessary info from SAP2000.
- These functions remain the same for all the commercial software.
- Simple features (ex. open, save, close program etc. )
- Specific features (ex. get FE name, add section & material property, etc. )
- Dll libraries perform computations.
- In each iteration there is interaction between HP-TOCP and the static program.

# Preprocessing

## Basic features

- Define the initial structure, boundaries and load condition in SAP2000 model.
- The first step of HP-TOCP is to collect all the geometrical information.
- Apply SIMP by defining a finite ( $k$ ) number of material properties.
- The modified equation of the Young Modulus is :  $E = E_{min} + (E_0 - E_{min}) * 1/k$
- Create ( $k$ ) number of section properties, so everyone has a different material.
- Correspond densities to the right section property.
- Update function:  $index = Convert.ToInt32(x^p * (k - 1))$



# Preprocessing

Specific features

## Filter

- Centroid of each element is computed
- Compute distances between each element and its neighbors
- Create a matrix with the convolution operator of each element

## Optimized – Non optimized areas

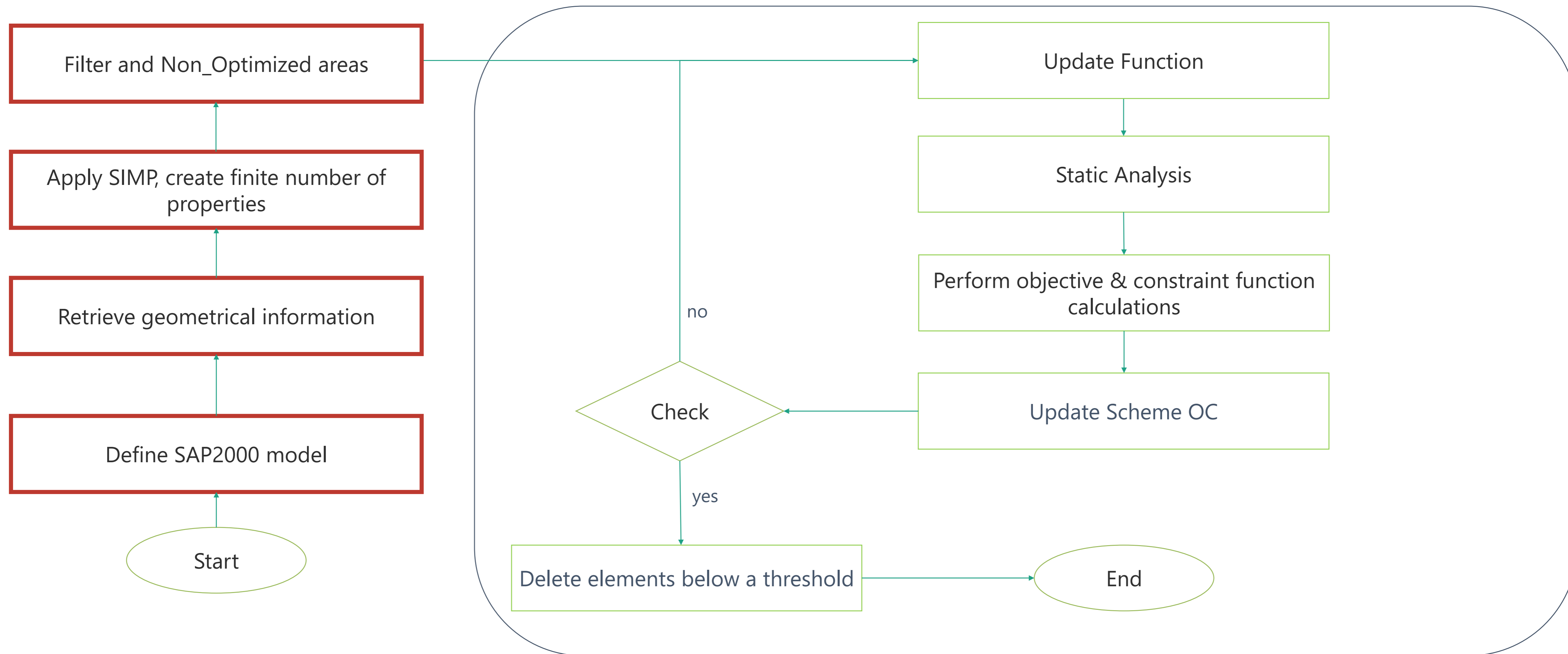
- Define a Group of FE named “Non\_Optimized” and assign the desired elements
- Define whether this area is void or full
- HP-TOCP recognize the areas and exclude them from the density update

# Iterative Procedure

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- Assign the right properties using the Update function
- Perform the Static Analysis
- Retrieve Analysis Results using delegates functions
- Compute Compliance, Derivative and volume
- Apply OC update scheme
- Threshold that indicates that a material doesn't exist
- Delete the equivalent elements

# Flowchart

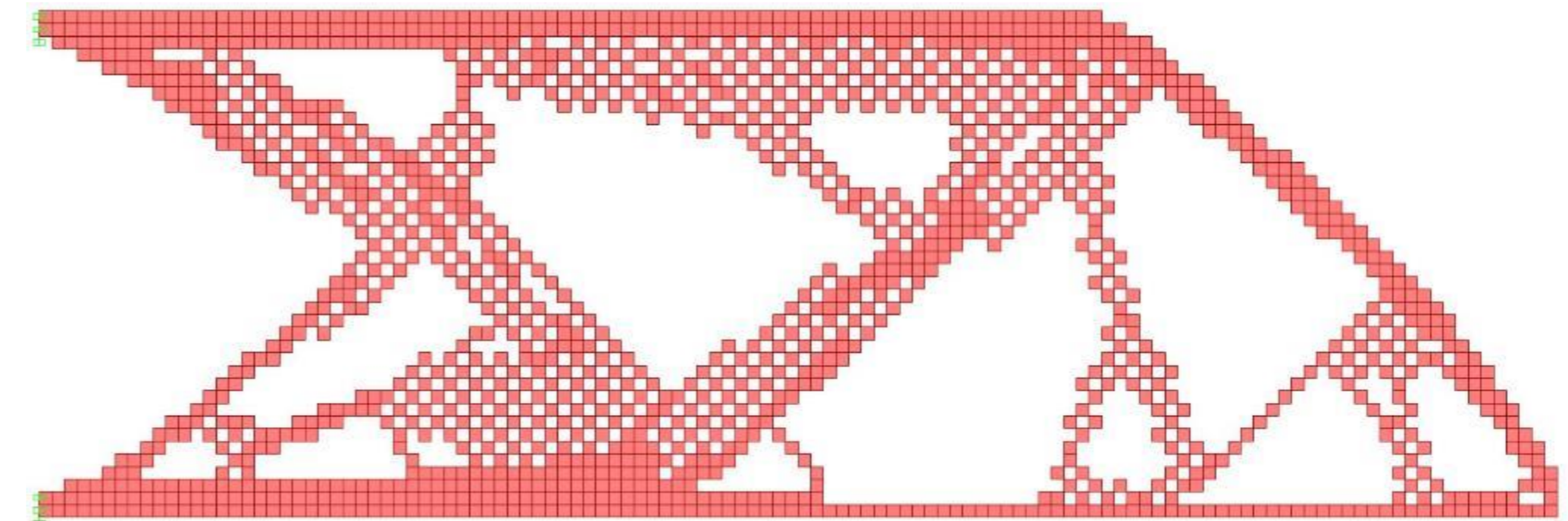


# 2D Test Cases

## Cantilever beam problem

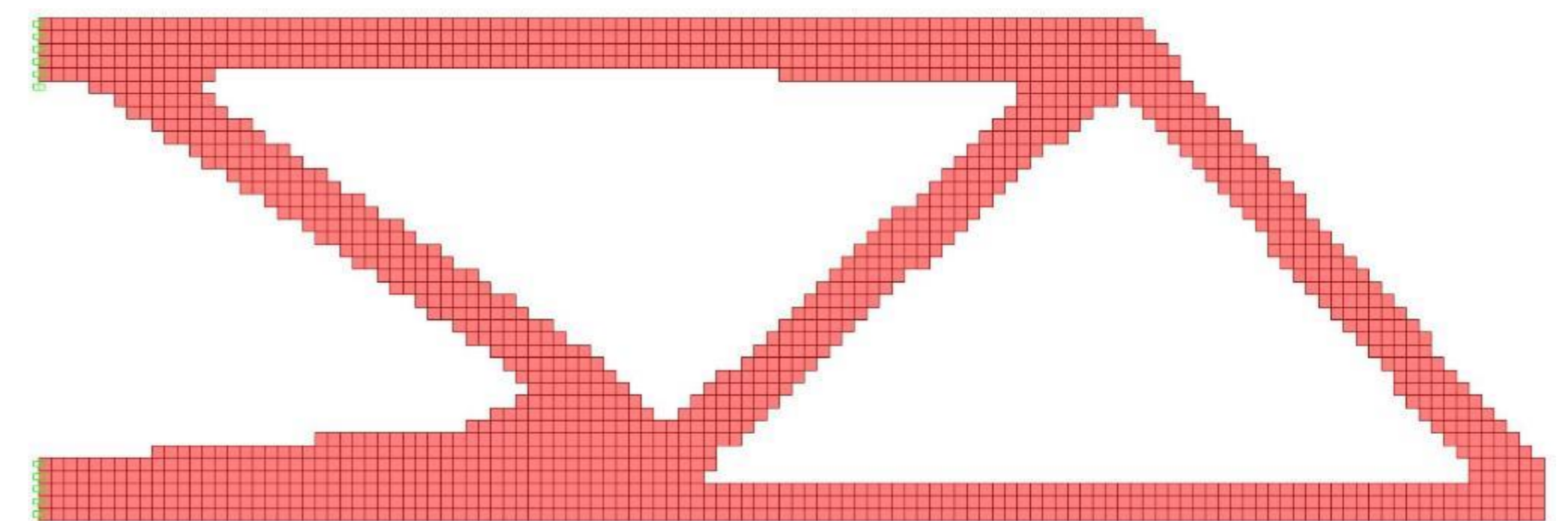
Initial domain

No filter



(a)

(b)  
Filter



(c)

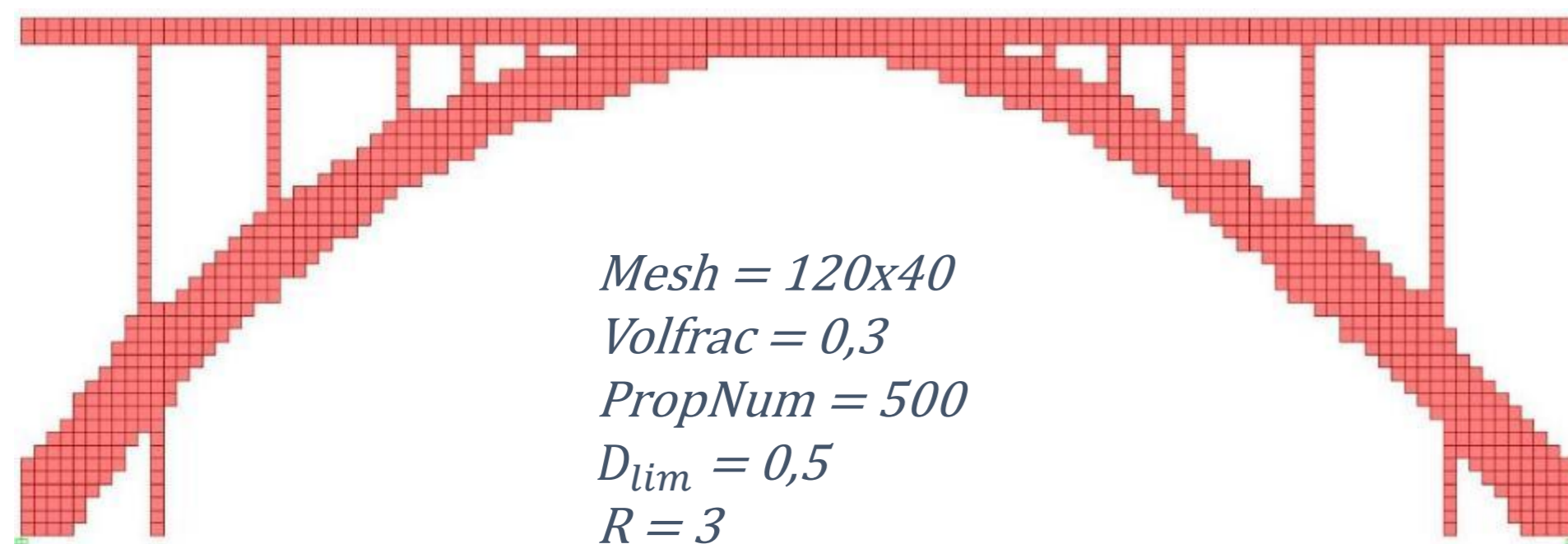
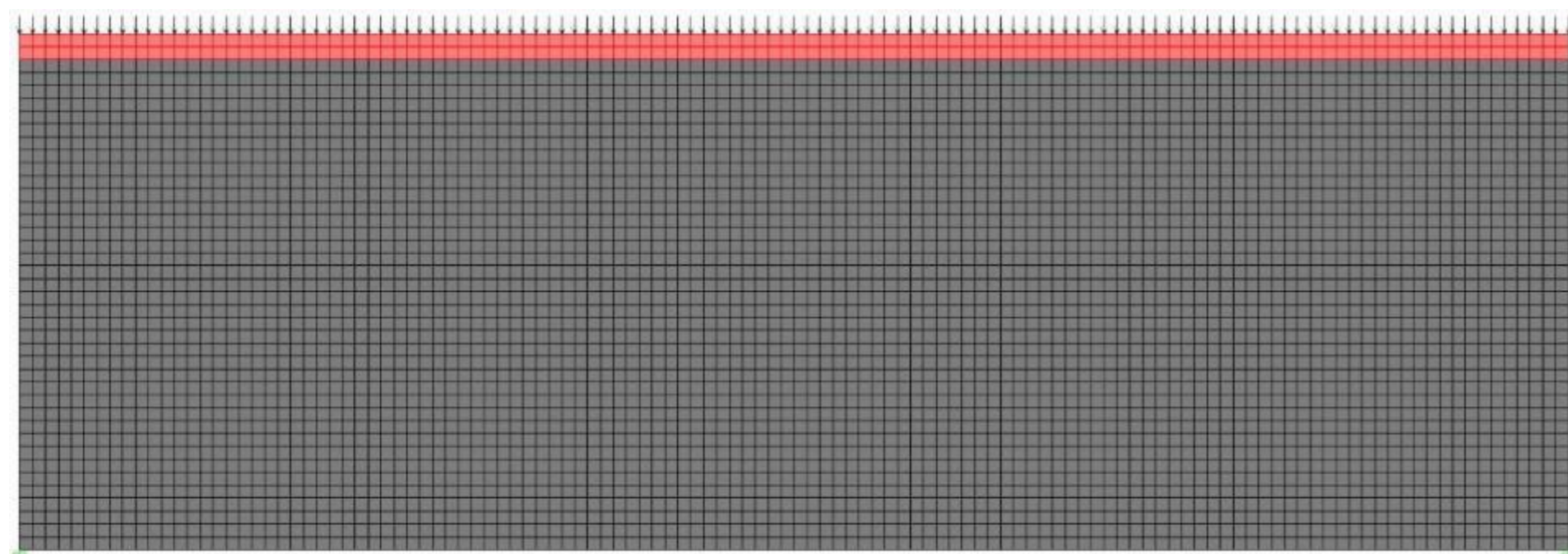
*Mesh = 120x40*  
*Volfrac = 0,3*  
*PropNum = 500*  
*D<sub>lim</sub> = 0,4*  
*R = 3*

*D<sub>lim</sub> = Limit density for deleting area elements*  
*PropNum = Section and material properties number*  
*R = Radius Filter*

# 2D Test Cases

Non optimized – Multiple loads

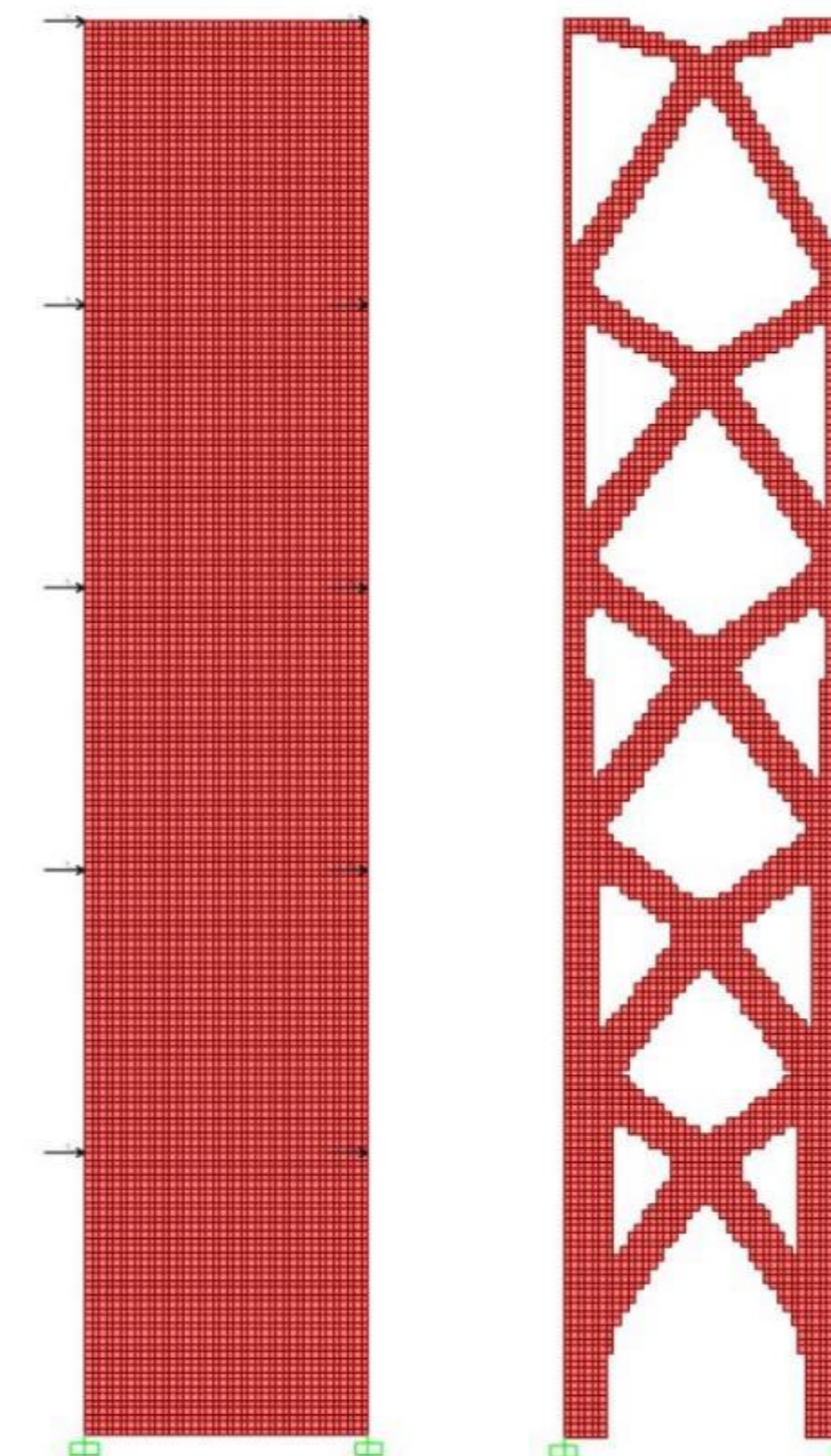
Bridge test case



*Mesh = 120x40*  
*Volfrac = 0,3*  
*PropNum = 500*  
*D<sub>lim</sub> = 0,5*  
*R = 3*

(b)

MRF test case



*Mesh = 40x200*  
*Volfrac = 0,3*  
*PropNum = 500*  
*D<sub>lim</sub> = 0,2*  
*R = 3*

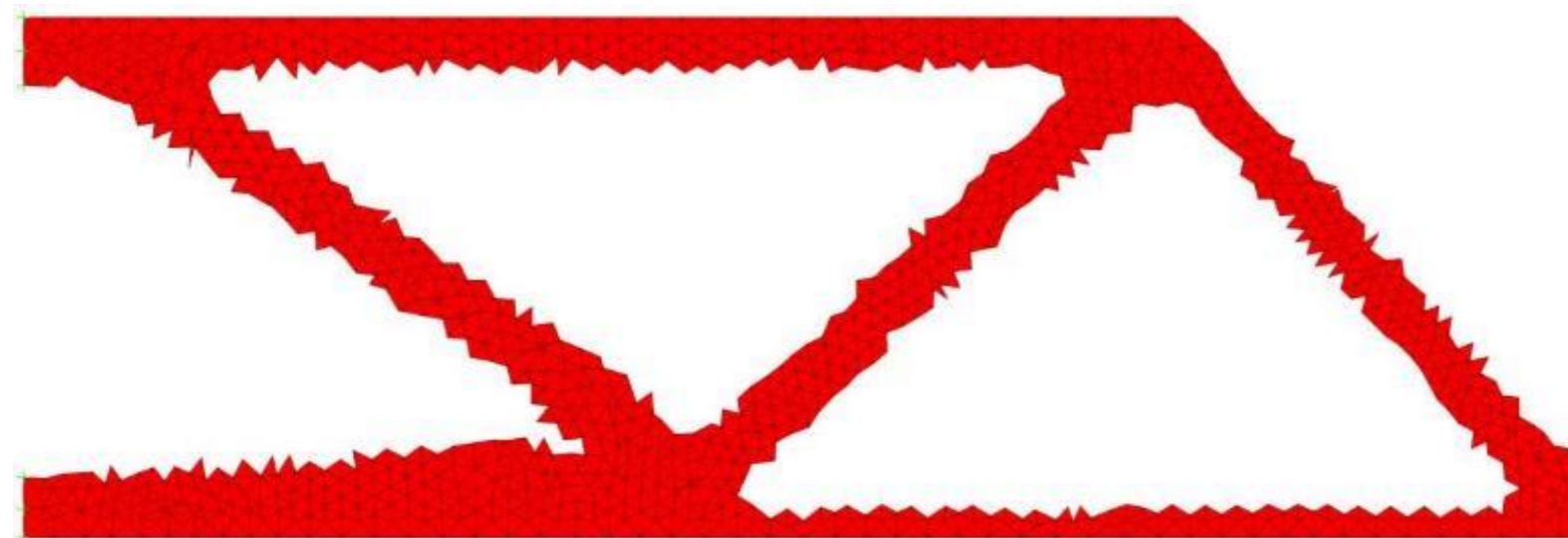
(b)

# Unstructured mesh & Plate case

## Cantilever beam

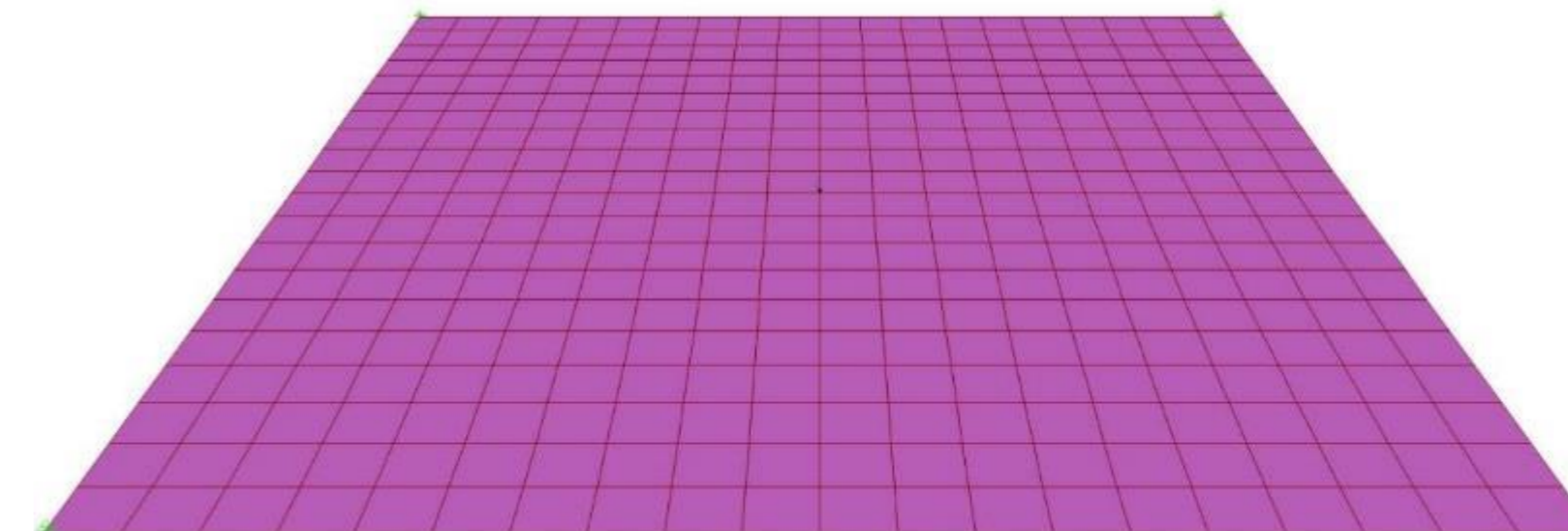


*Unstructured mesh: 5000 elements*  
*Volfrac = 0,3*  
*PropNum = 500*  
 *$D_{lim} = 0,5$*   
 *$R = 3$*

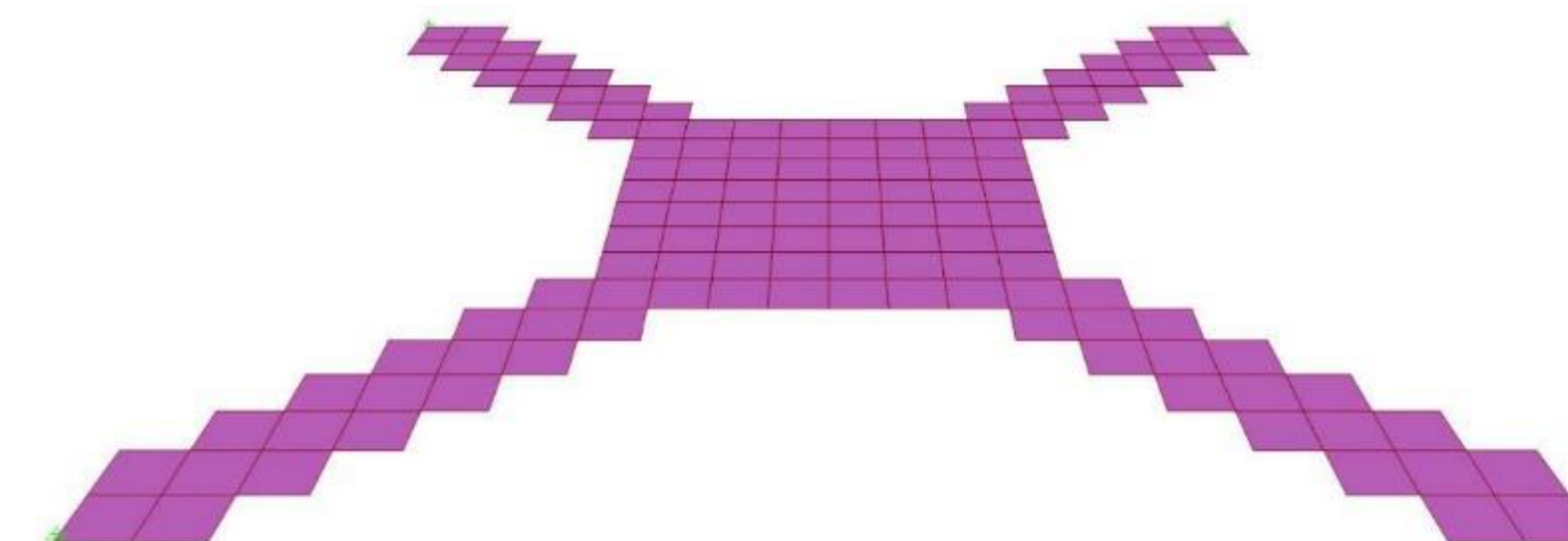


(a)

## Simple plate



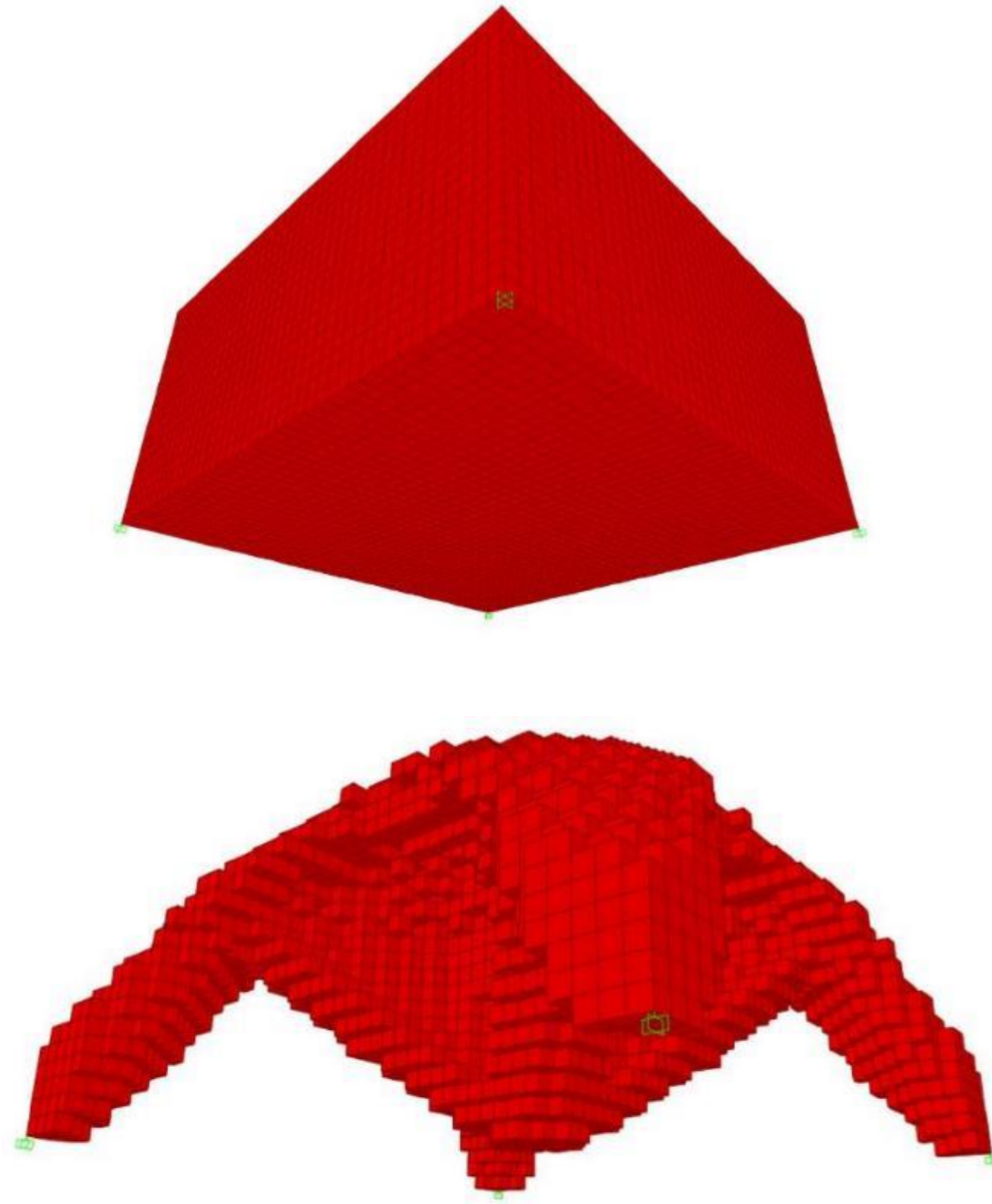
*Mesh = 20x20*  
*Volfrac = 0,3*  
*PropNum = 500*  
 *$D_{lim} = 0,4$*   
 *$R = 3$*



(b)

# 3D test cases

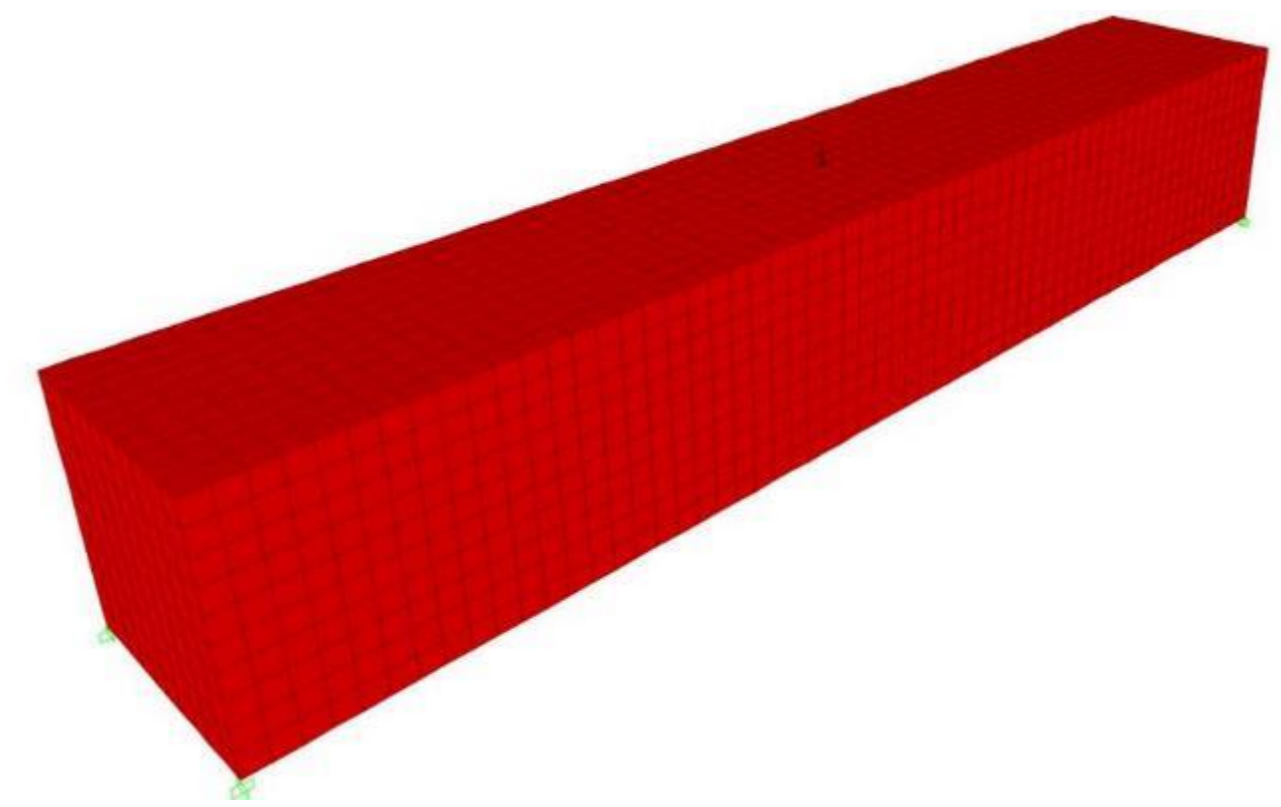
3D Wheel



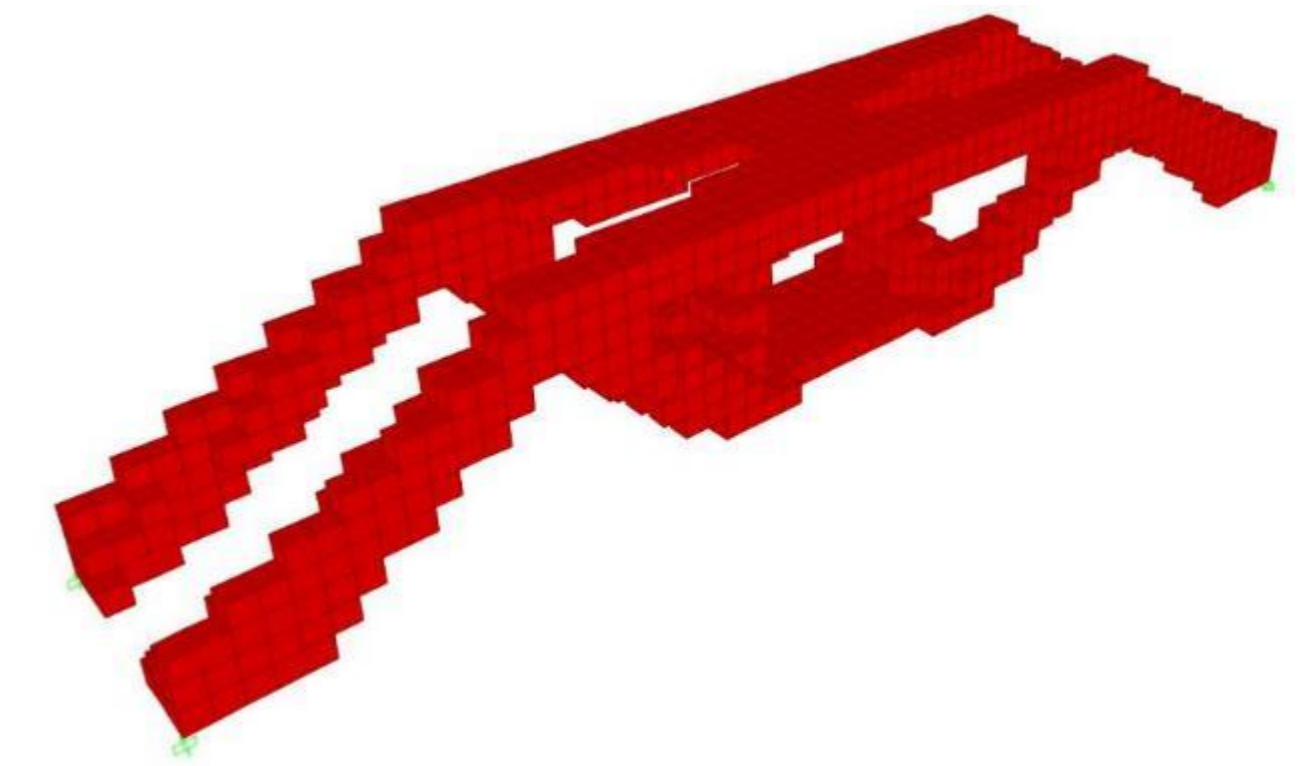
(a)

$Mesh = 40 \times 40 \times 20$   
 $Volfrac = 0,2$   
 $PropNum = 500$   
 $D_{lim} = 0,4$   
 $R = 3$

MBB beam



$Mesh = 120 \times 40$   
 $Volfrac = 0,3$   
 $PropNum = 500$   
 $D_{lim} = 0,5$   
 $R = 3$



(b)

# Conclusion

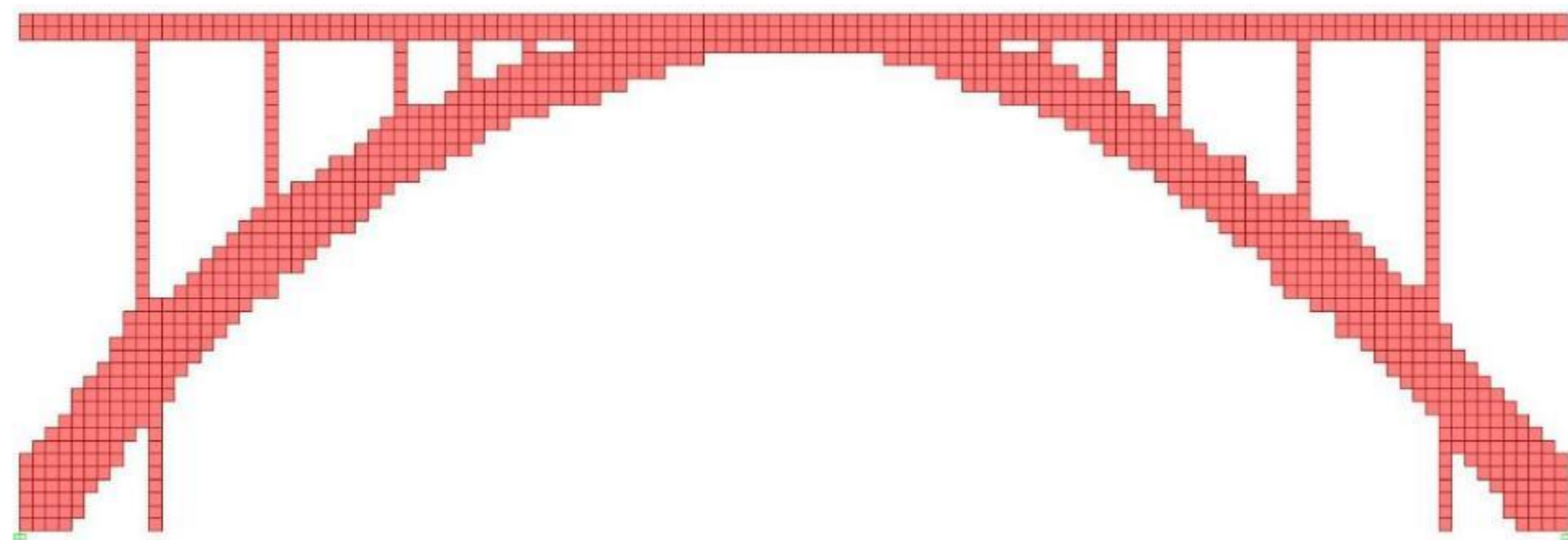
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- HP –TOCP independent of the static software
- Integration with SAP2000
- SIMP method, OC algorithm
- Special features (Filter, Non\_optimized areas and multiple load cases)
- Independent of the mesh and finite element type
- 2D structured and unstructured test cases
- Plate and 3D problems



# Thank You

Questions?



#### ACKNOWLEDGMENTS

This research has been co-financed by the European Union and Greek national funds through the Operational Program Competitiveness, Entrepreneurship and Innovation, under the call RESEARCH – CREATE – INNOVATE (project code: T1EDK-05603-"HP-OCP" - Holistic, High Performance Optimization Computing Platform»

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ΕΠΙΧΕΙΡΗΜΑΤΙΚΟΤΗΤΑ  
ΚΑΙΝΟΤΟΜΙΑ



## Σχόλια - Προβλήματα - Παρατηρήσεις

Δεν υπήρχαν παρατηρήσεις

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Ημ/νία :	31/01/2020	31/01/2020